

NAVIGATION OF MOBILE ROBOTS

Maria Isabel Ribeiro
Pedro Lima

mir@isr.ist.utl.pt

pal@isr.ist.utl.pt

Instituto Superior Técnico (IST)
Instituto de Sistemas e Robótica (ISR)
Av. Rovisco Pais, 1
1049-001 Lisboa
PORTUGAL

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- J. Borenstein, H. R. Everett, L. Feng, “Where Am I?”, Technical Report, University of Michigan. (Chapter 6)

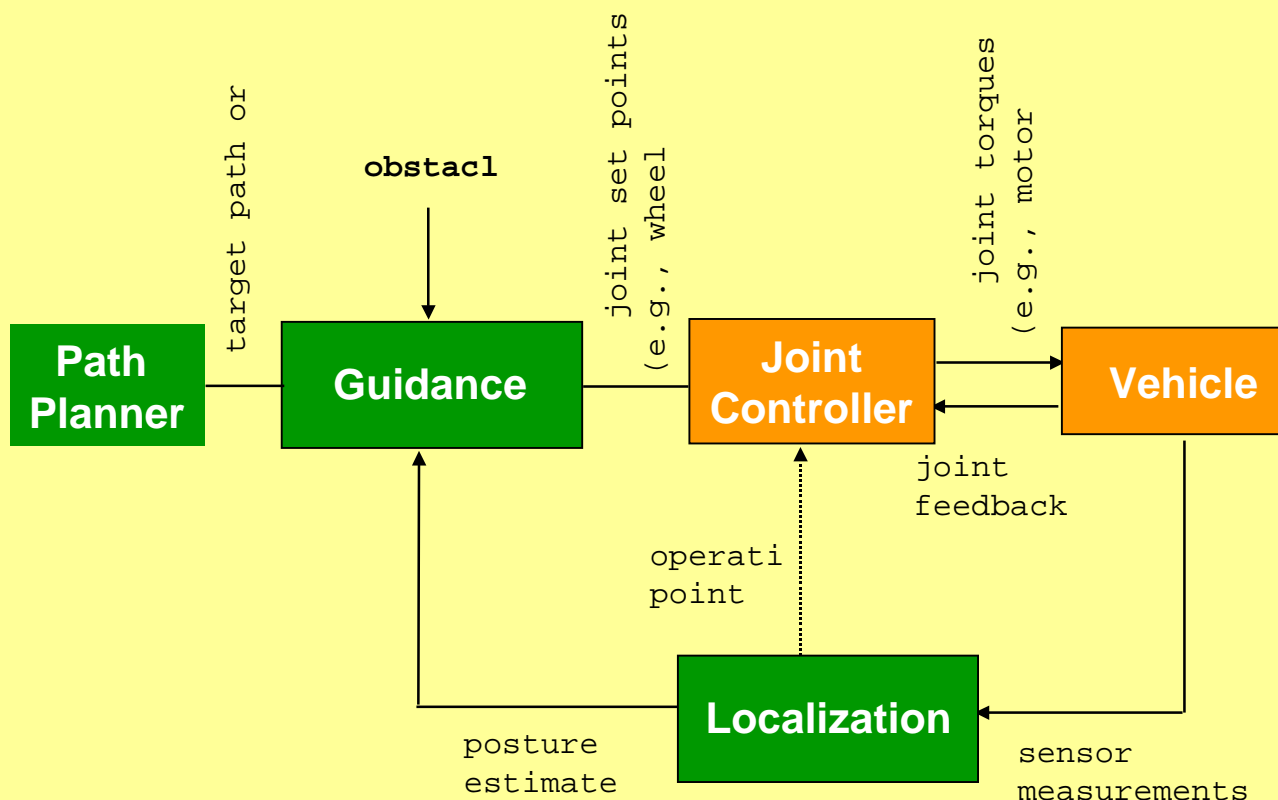
The Navigation Problem

NAVIGATION

Process used by a mobile robot to move from an initial pose to a final pose with respect to an initial frame

Key Questions:

- ✚ Where am I ?
- ✚ Where am I going ?
- ✚ How should I get there ?



- **GUIDANCE**

- take the robot from the current posture desired posture, possibly following a determined path or trajectory, while obstacles

Some Guidance methodologies

- **State(posture)-feedback methods:**
 - **posture stabilization** (initial and final postures given; no path or trajectory pre-determined; obstacles not considered; may lead to large unexpected paths)
 - **trajectory tracking** (requires pre-planned path)
 - **virtual vehicle tracking** (requires pre-planned trajectory)
- **Potential-Field like methods**
 - **potential fields** (holonomic vehicles)
 - **generalized potential fields** (non-holonomic vehicles)
 - **modified potential fields** (non-holonomic vehicles)
- **Vector Field Histogram (VHF) like methods**
 - **nearness diagram navigation** (holonomic vehicles)
 - **freezone** (non-holonomic vehicles)

• LOCALIZATION

- Determine the posture (position + the robot at each time instant

Some Localization methodologies



Relative Localization (Localization with relative measurements)

- Odometry

Mobile robot localization through wheel motion evaluation

- Inertial Navigation

Mobile robot localization through its motion state evaluation (velocities and accelerations)

Dead-reckoning



Absolute Localization

- Active beacons

Computes absolute location by measuring the direction of incidence (or the distance to) 3 or more active beacons. Transmitter locations must be known in inertial frame

- Artificial and Natural Landmarks

Landmarks are located in known environment places, or they are detected in the environment. Same method used for active beacons applies.

- Model matching

Information from robot sensors is compared to a map or world model. Matching sensor-based and world model maps, vehicle's absolute pose is estimated

This can be used to update the world map over time



Relative Localization + Absolute Localization

- Uses encoders to measure the distance traveled by each wheel
 - From the robot kinematics the translation and rotation of the robot frame relative to the world frame is evaluated
- Absolute pose estimation results from the integration of relative translation and orientation between two encoder readings.
- Odometry performance is a function of the vehicle's kinematics

- **Errors in odometry**

- Systematic Errors

important as they lead to additive errors

**In regular terrain, they are more important than non-systematic errors
they depend on the robot and/or sensors characteristics**

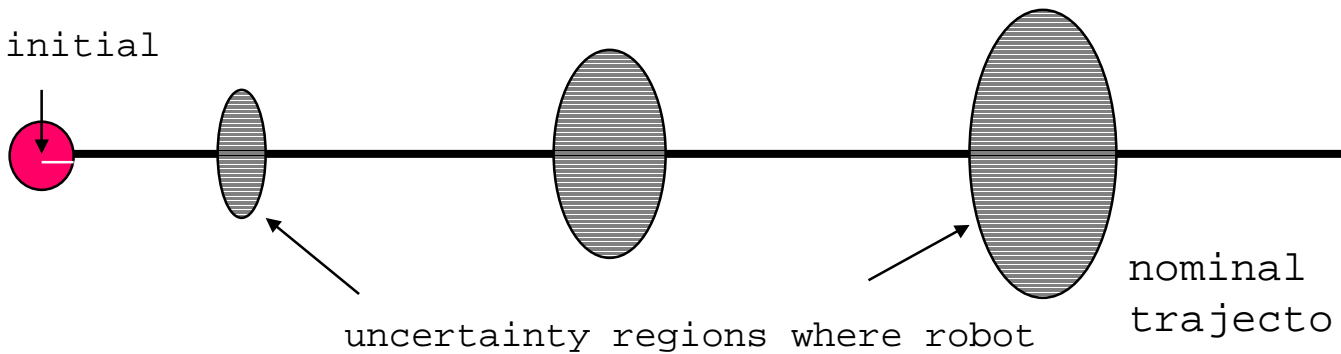
- different wheel diameters
 - mean wheel diameter differs from the nominal
 - unaligned wheels
 - finite encoder resolution and sampling time

- Non-systematic Errors

in irregular terrains these may be the most important errors

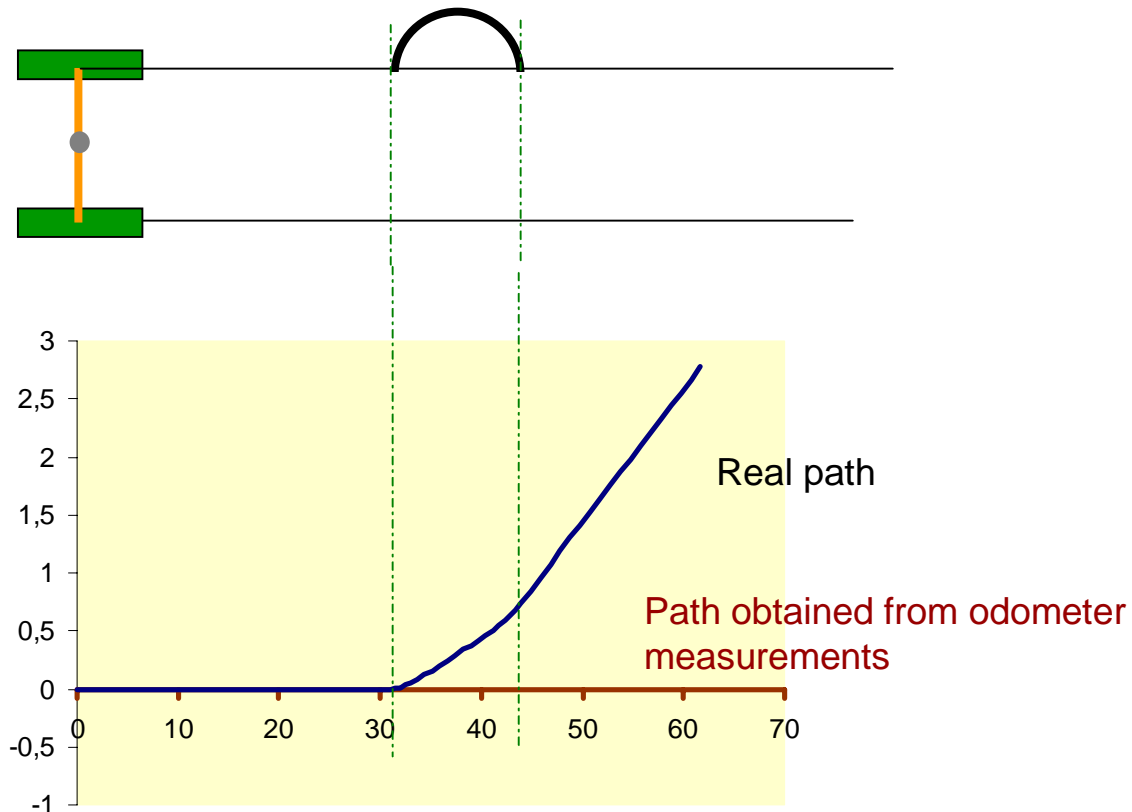
- motion on irregular surfaces
 - Motion over unexpected obstacles
 - Wheel slippage
 - solo escorregadio
 - Large vehicle's accelerations
 - Quick rotations
 - External forces (interaction with external obstacle))
 - Internal forces (free wheels)
 - Wheel non point contact

Odometry Errors



Typical Errors for a Differential Drive Robot

- Motion command – equal velocities in both wheels
- Surface profile



See a set of Handouts on Odometry

- Active Beacons
 - Most common navigation aids on ships and airplanes
 - Provide very accurate positioning information with minimal processing
 - High cost in installation and maintenance
- Two different types of active beacon systems:
 - **Trilateration**
 - **Triangulation**

TRILATERATION

Determination of vehicle's pose based on distance measurements to known beacon sources

Usual configuration

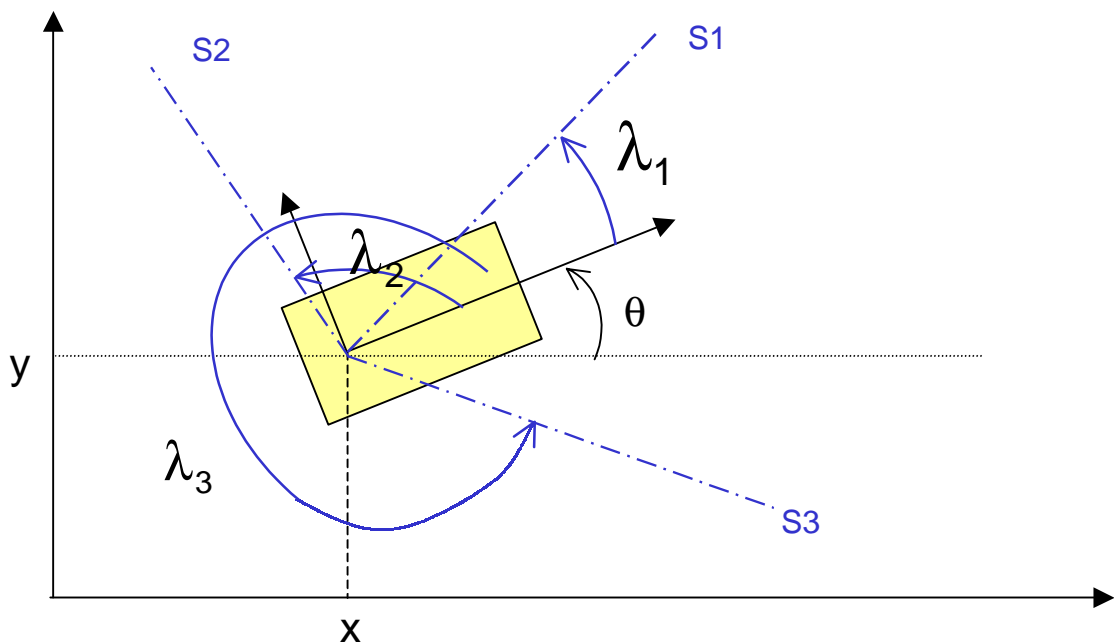
- 3 or more transmitters mounted at known locations in the environment and one receiver on board the robot
- one transmitter on-board and receivers mounted on the environment

Examples

- GPS

TRIANGULATION

- Determination of vehicle's pose (x, y, θ) based on the evaluation of the angles, $\lambda_1, \lambda_2, \lambda_3$ between the robot longitudinal axis and the direction with which three beacons installed on the environment at known positions are detected.



TRIANGULATION

is a common ranging technique
with its origins in ancient Greek
and Egiptian civilizations

(used for ship navigation, civil engineering)



TRIANGULATION method obtains the **distance** to an object
by simple geometric calculations

Result of trigonometry

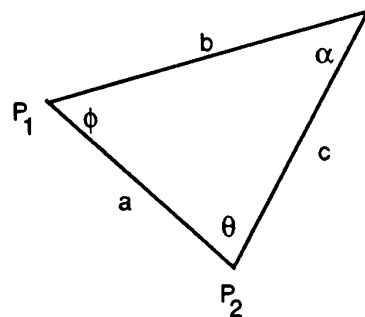
Given

the length of a side of a triangle

(a)

two angles of the triangle

(ϕ , θ)



It is possible to determine

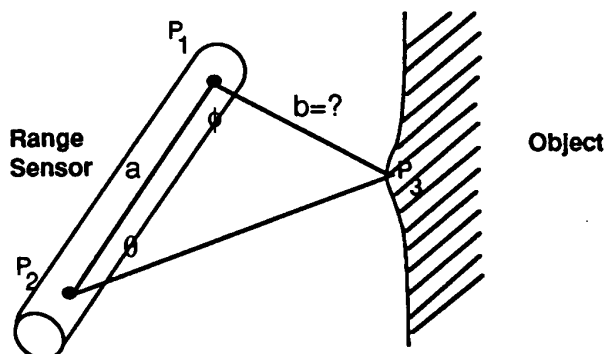
the length of the remaining sides

(b, c)

the remaining angle

(α)

$$b = a \cdot \frac{\sin \theta}{\sin (\theta + \phi)}$$



Example

Stereo Vision